

PHD DEFENSE

# Contribution to prognostics of PEM fuel cells: approaches based on degradation information at multiple levels

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Presented by  
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Advisors  
**Catherine CADET**  
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**Nadia YOUSFI-STEINER**

January 18, 2018



# Outline

- 1 Background & motivation

## ADAPTING THE STATE OF THE ART:

- 2 Remaining Useful Life prediction of PEM fuel cells
  - ▶ Particle Filtering-based RUL prediction
  - ▶ Taking into account reversible degradation

## BEYOND THE STATE OF THE ART:

- 3 Multi-level prognostics using online inspection of degradation covariates
- 4 Multi-level prognostics using different sources of degradation information
- 5 Conclusion & perspectives

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# Part I

## Background & Motivation

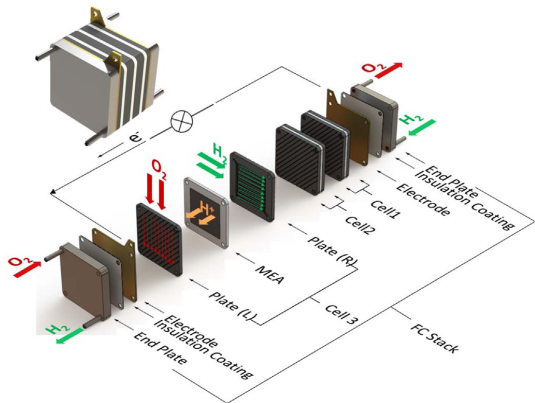


# Proton Exchange Membrane (PEM) fuel cell

- ▶ Energy transition  
Hydrogen
- ▶ Promising alternative transition device  
Fuel Cells
- ▶ PEM Fuel Cell
  - ▶ Low temperature  $80^{\circ}C-100^{\circ}C$
  - ▶ Small size  
Single cell :  $100\text{ cm}^2$   
 $P \approx 0.4\text{ W/cm}^2$
  - ▶ High efficiency  
 $\eta \approx 70\%$
  - ▶ Tailorable power
  - ...



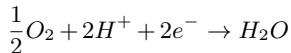
# Stack and cell



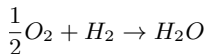
► **Anode:**



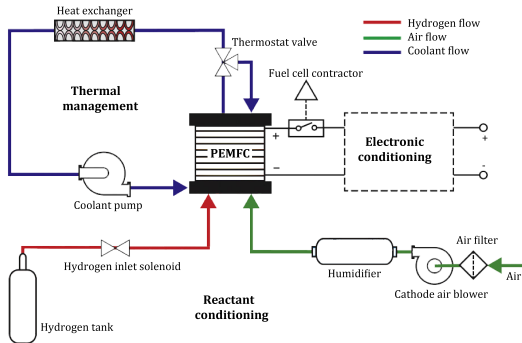
► **Cathode:**



► **Overall:**



# Balance of Plant



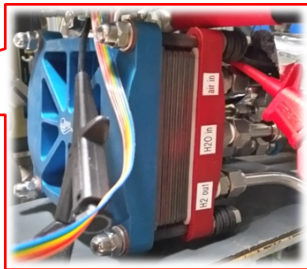
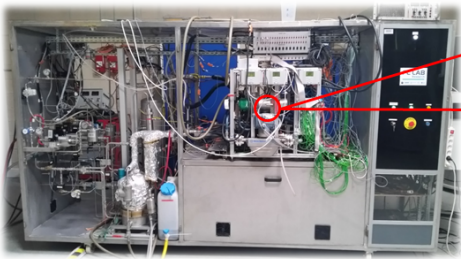
## Subsystems

- ▶ Reactant conditioning *tank, pumps, valves, ...*
- ▶ Electronic conditioning *regulator, controller, ...*
- ▶ Thermal management *heat exchanger, ...*

# Balance of Plant

Heat exchanger

## A PEM fuel cell test bench in FCLAB



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# Challenges

## Issues

- ▶ Poor health management (Faults)
- ▶ Materials and interfaces degradation (Aging)

## Consequences

- ▶ Performance degradation
- ▶ Lifespan limitation

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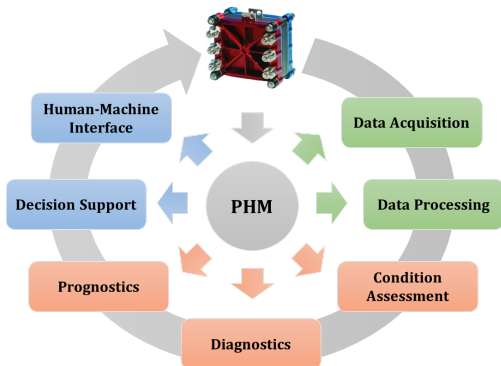
## Challenges

- ▶ Enhance reliability
- ▶ Better manage lifespan

⇒ Prognostic and Health Management

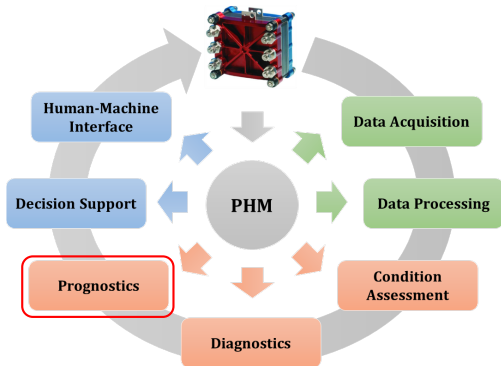
# Prognostics and Health Management (PHM)

- ▶ Recent dynamic approach to **monitor**, **analyze** and **master** the Remaining Useful Life (RUL) of industrial systems
- ▶ Pioneering technique in fuel cells technologies



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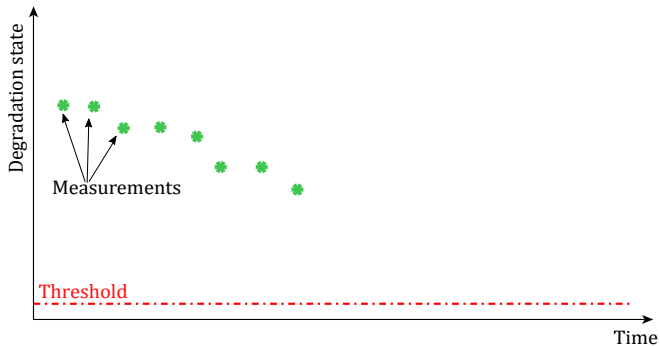


# Remaining Useful Life (RUL)

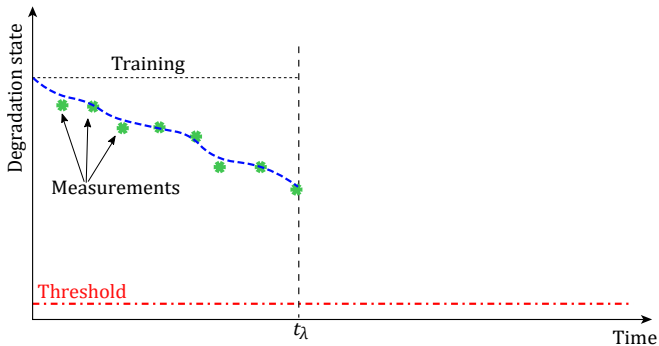
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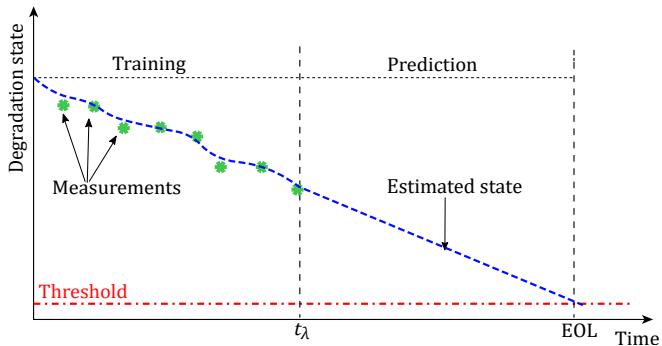
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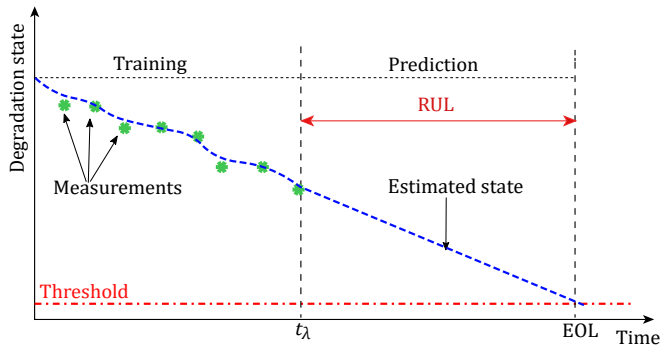
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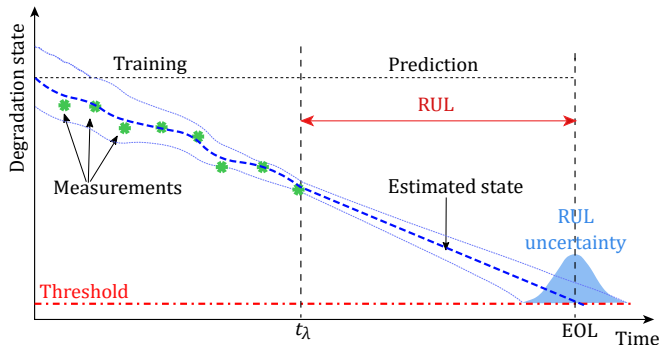
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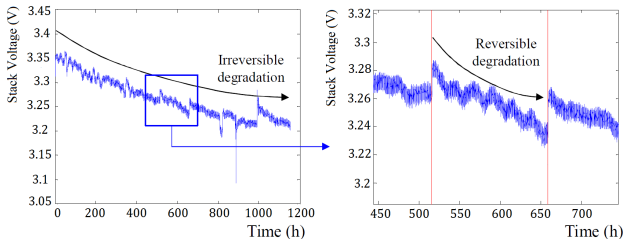
# Remaining Useful Life (RUL)



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# Difficulties



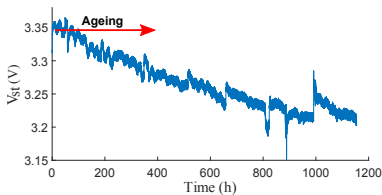
- ▶ Degradation can be different:
  - ▶ irreversible (*e.g.* due to material deterioration)
  - ▶ reversible (*e.g.* due to operating conditions)
- ▶ Degradation can be generated at different levels

⇒ Observed from different measurements

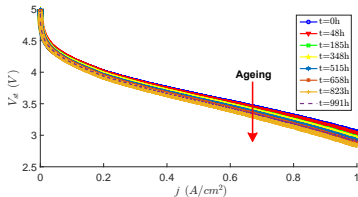


# Degradation measurements

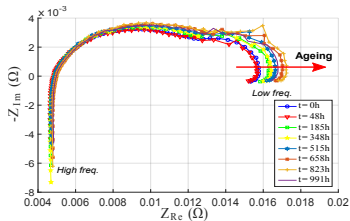
## Stack voltage (or power)



## Polarization curves



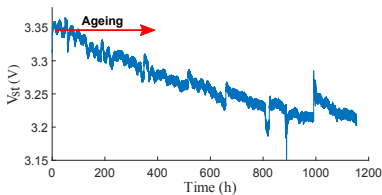
## Electrochemical Impedance Spectroscopy (EIS)



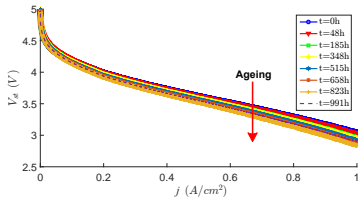
- ▶ Classical measurements  
*Voltage, Power*
- ▶ State of Health (SOH) measurements  
*EIS, Polarization*

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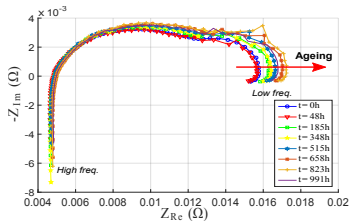
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## Electrochemical Impedance Spectroscopy (EIS)



- ▶ Classical measurements  
*Voltage, Power*
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⇒ Use multiple measurements

# Objectives and contributions

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- 1 RUL prediction (on real application data) with taking into account both irreversible and reversible degradation

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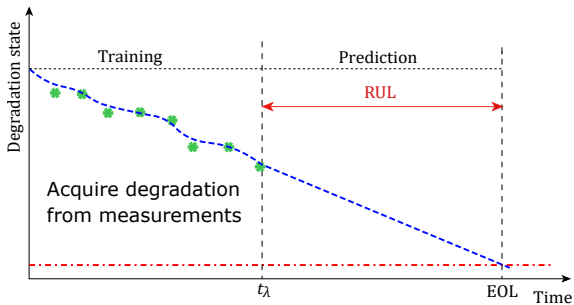
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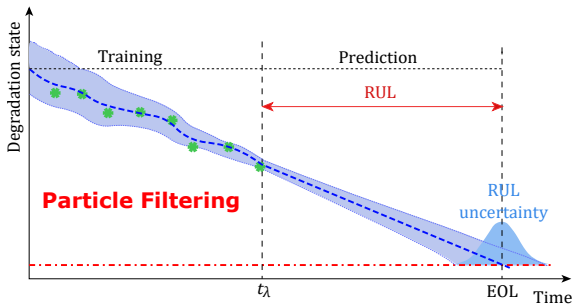
## Part II

# Remaining Useful Life Prediction of PEM fuel cell

# Particle Filtering-based prognostics



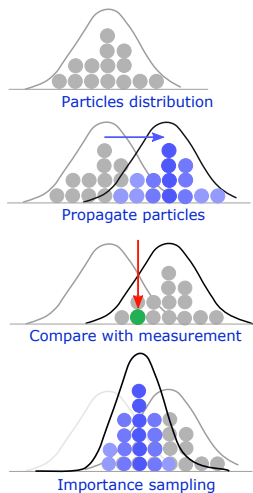
# Particle Filtering-based prognostics



Estimator uses large amount of randomness to approach the truth

- ▶ Technique for implementing Recursive Bayesian filter by Monte Carlo sampling
- ▶ Nonlinear, non Gaussian model tracking

# Particle Filtering (PF)



Particles with corresponding weights are used to form an approximation of PDF

- 1 Split initial state into particles

$$x_{t-1} \rightarrow \{x_{t-1}^i\}_{i=1}^N$$

- 2 Propagate particles through the transition function

$$x_t^i = f(x_{t-1}^i, \omega_{t-1}^i) \rightarrow p(x_t | x_{t-1})$$

- 3 Importance sampling

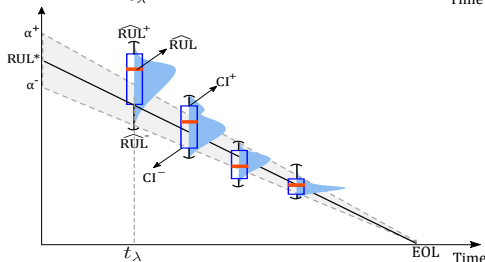
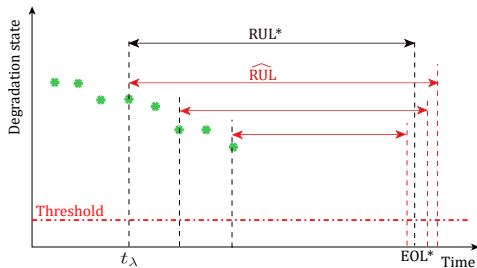
$$W_t^i \propto p(z_t | x_t^i) \rightarrow x_t^{i*}$$

- 4 Re-sampling

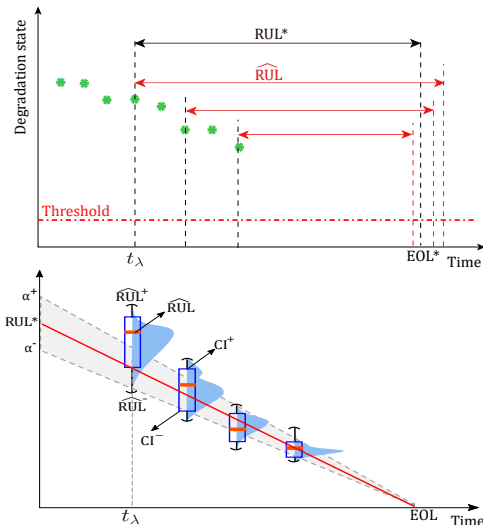
$$\{x_{t-1}^{i*}\}_{i=1}^N \rightarrow p(x_t^* | z_t)$$

# Prognostic performance

## Prognostic metrics



# Prognostic performance

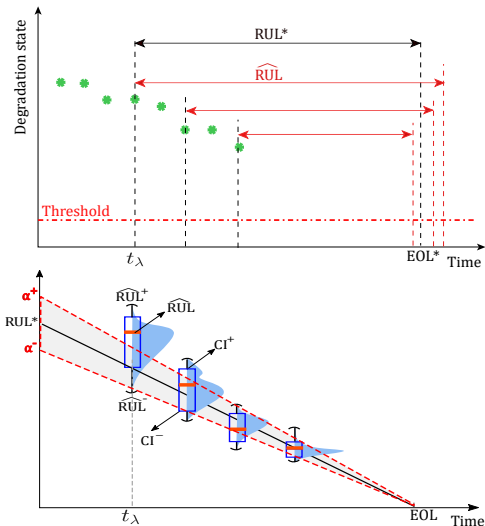


## Prognostic metrics

- Accuracy index

$$Acc_\lambda = 1 - \frac{|RUL_\lambda^* - \widehat{RUL}_\lambda|}{RUL_\lambda^*}$$

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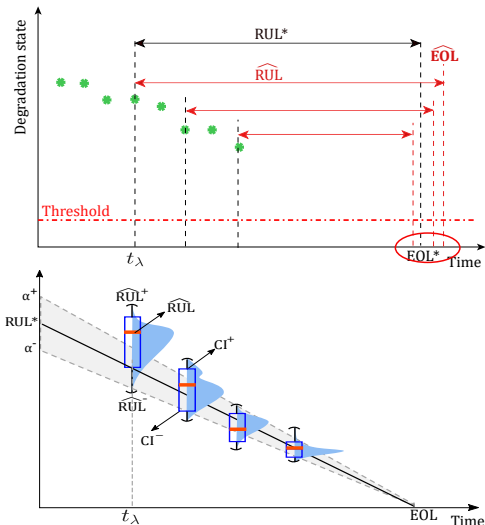
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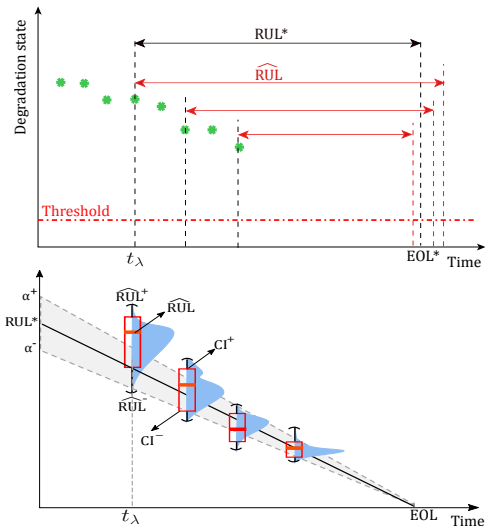
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- Steadiness index

$$Std_\lambda = \frac{\sqrt{\text{var}(\widehat{EOL}_{(\lambda-L):\lambda})}}{EOL^*}$$

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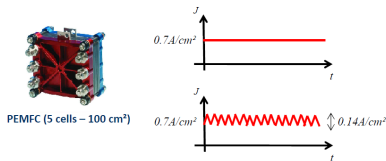
- Precision index

$$Prec_\lambda = \frac{\widehat{RUL}_\lambda^{CI^+} - \widehat{RUL}_\lambda^{CI^-}}{RUL_\lambda^*}$$

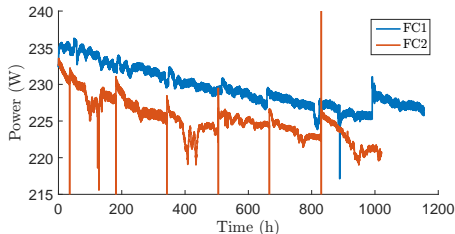
## Application data (test bench FCLAB)

- ▶ Two PEM fuel cell stacks under operation degrade
- ▶ Stack power measurements are used as the degradation indicator

FC1 - Long-term test without current ripples



FC2 - Long-term test with high frequencies current ripples



## Application data (test bench FCLAB)

- ▶ Two PEM fuel cell stacks under operation degrade
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### Degradation state models

- ▶ Pure logarithmic:

$$x_k = -\alpha \cdot \ln(t_k/t_{k-1}) + x_{k-1}$$

- ▶ Log-linear:

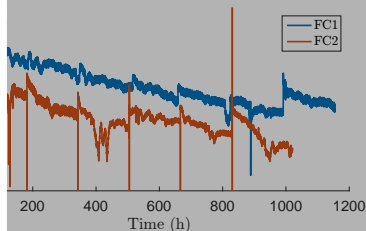
$$x_k = -\alpha \cdot \ln(t_k/t_{k-1}) - \beta \cdot (t_k - t_{k-1}) + x_{k-1}$$

- ▶ Linear:

$$x_k = -\beta \cdot (t_k - t_{k-1}) + x_{k-1}$$

- ▶ Polynomial:

$$x_k = \alpha \cdot (t_k - t_{k-1})^2 - \beta \cdot (t_k - t_{k-1}) + x_{k-1}$$



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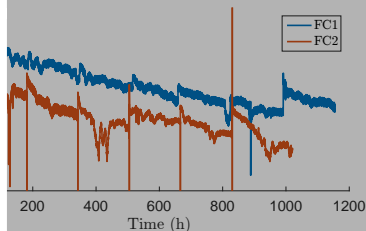
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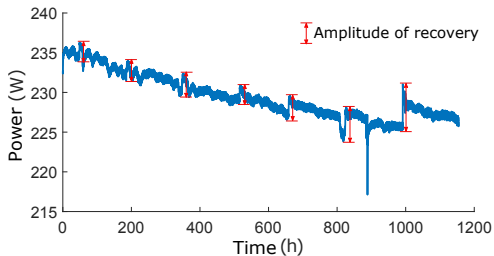
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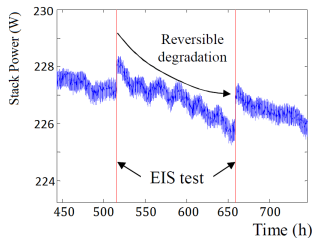
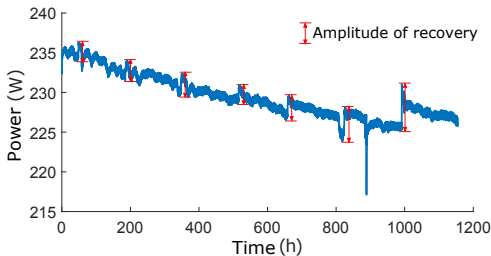
# Difficulty

## Reversible degradation



# Difficulty

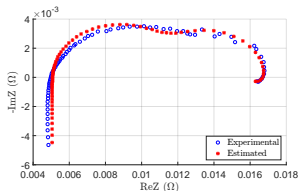
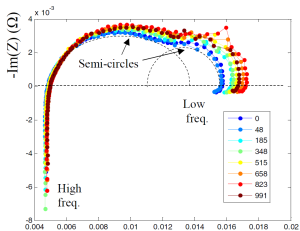
## Reversible degradation



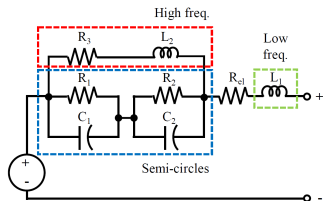
Use information from characterization measurement  
⇒ Electrochemical Impedance Spectroscopy

# Electrochemical Impedance Spectroscopy (EIS) data

## EIS measurements



## Equivalent Circuit Model <sup>1</sup>



## Polarization resistance

$$R_{pol} = \frac{(R_1 + R_2) \cdot R_3}{R_1 + R_2 + R_3} + R_{el}$$

<sup>1</sup> Kim, T. et al., (2014). A degenerated equivalent circuit model and hybrid prediction for state-of-health (SOH) of PEM fuel cell. In: *2014 International Conference on Prognostics and Health Management*. pp. 1-7.



# State transition model

## Hypothesis

- ▶ Reversible degradation is related to  $R_{pol}$
- ▶  $R_{pol}$  can be estimated from EIS

$$x_c = x_k + \alpha_1(R_{pol}) \cdot \exp(-\beta_1(R_{pol}) \cdot (t_k - t_{k-1}))$$

$$x_k = \alpha \cdot (t_k - t_{k-1})^2 - \beta \cdot (t_k - t_{k-1}) + x_{k-1}$$

# State transition model

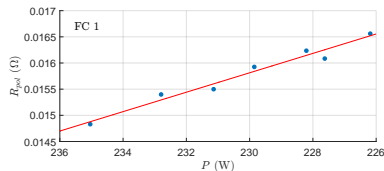
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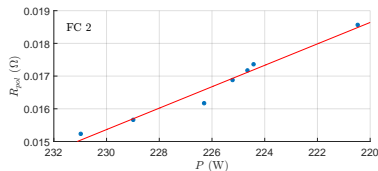
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### $R_{pol}$ vs. Power (FC1)



### $R_{pol}$ vs. Power (FC2)



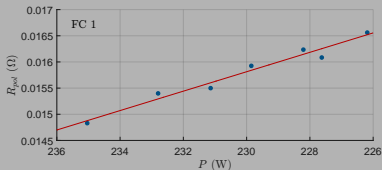
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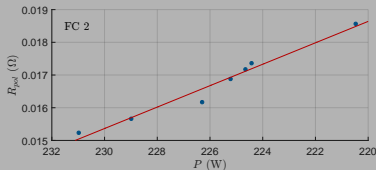
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$$x_c = x_k + \alpha_1 \cdot \frac{R_{pol}(c)}{R_{pol}(0)} \cdot \exp\left(-\beta_1 \cdot \frac{R_{pol}(c)}{R_{pol}(0)} \cdot (t_k - t_{k-1})\right)$$

$R_{pol}$  vs. Power (FC1)

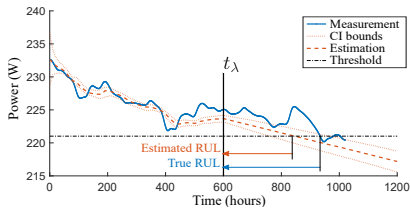


$R_{pol}$  vs. Power (FC2)

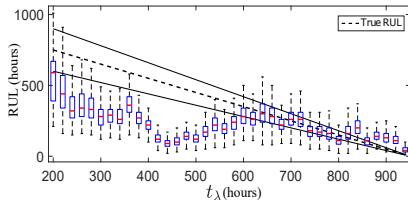


# Results (FC2)

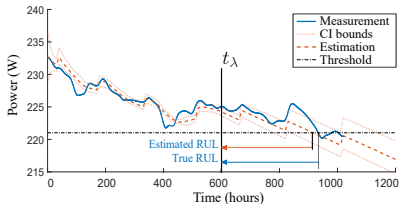
## Estimation with classical model



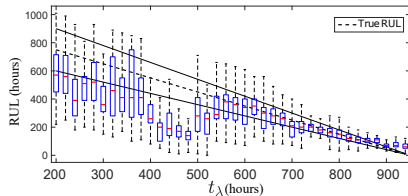
## RUL predictions with classical model



## Estimation with proposed model

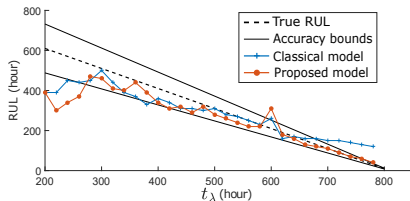


## RUL predictions with proposed model

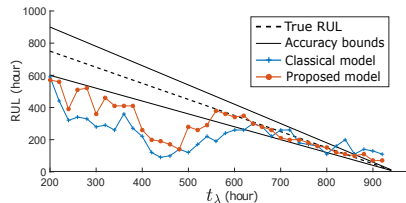


# Prognostic performance

## RUL predictions of FC1



## RUL predictions of FC2



## Performance metrics

	FC 1				FC 2			
	<i>Acc</i>	<i>aAc</i>	<i>Prc</i>	<i>Std</i>	<i>Acc</i>	<i>aAc</i>	<i>Prc</i>	<i>Std</i>
Classical	0.67	0.29	0.89	0.06	0.48	0.11	0.69	0.17
Proposed	0.86	0.42	0.68	0.06	0.72	0.34	0.74	0.12

## Summary

Challenge accomplished:

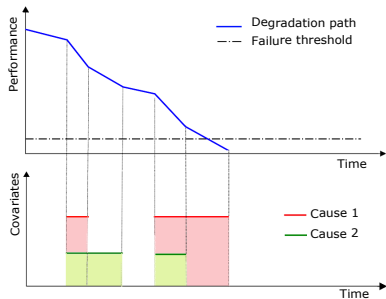
- ▶ RUL predictions of PEM fuel cell application with taking into reversible degradation
- ▶ Reversible degradation has been investigated by using the information of  $R_{pol}$
- ▶ Prediction quality has been improved by using additional information from SOH characterization

How to generalize the use of degradation related information  
⇒ Introduce **covariates** to the degradation model

## Part III

# Multi-level Prognostics Using Online Inspection of Degradation Covariates

# Problem statement



## Degradation

- ▶ Continuously monitored with simple measurements
- ▶ Affected by the change of covariates

## Assumption

Possible to inspect the covariates with extra cost

## Objective

Use the information of covariates for RUL prediction



# How?

Design a degradation covariate inspection scheme

- ▶ When and how to apply an inspection on covariates (that costs)
- ▶ Ensure the prognostic quality
- ▶ Minimize the inspection cost

# General modeling assumptions

## General modeling assumptions

- ▶ Evolution of the degradation follows a stochastic process:

$$x_k = f_k(x_{k-1}, \Theta_k)$$

- ▶ Impacts of covariates on the degradation model parameter can be quantified and modeled:

$$\Theta_k = g_k(c_k)$$

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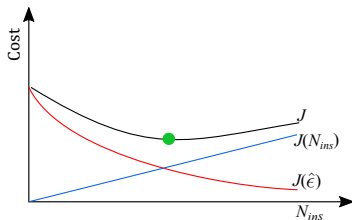
⇒ Possible to update the degradation model by inspecting the degradation covariate with **cost**

# Cost of the covariate inspection

## Global cost

$$J = J_{inspection}(N_{ins}) + J_{estimation}(\hat{\epsilon})$$

- ▶ Inspection incurs application cost
- ▶ Inaccurate estimation leads to prognostic quality cost



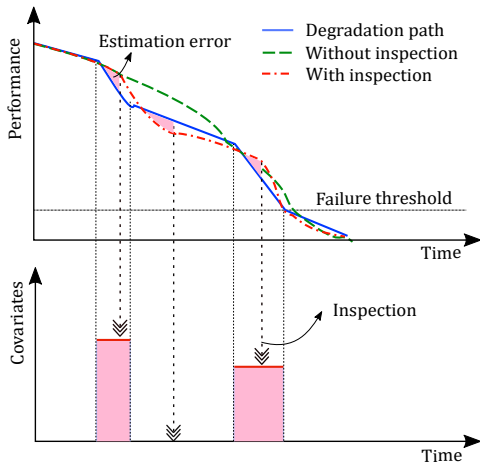
Find the optimal trade-off

## Method

Two decision variables:

- ▶ inter-inspection period  $\tau \rightarrow$  number of inspections  $N_{ins}$
- ▶ error threshold  $ET \rightarrow$  estimation error  $\hat{\epsilon}$

# Covariates inspection schemes



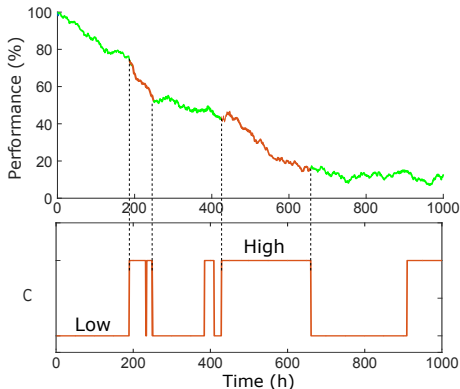
## Periodic inspection

Performed regularly at fixed time intervals  $\tau$

## Online inspection

Triggered online when the accumulated estimation error reaches an error threshold  $ET$

# Degradation example



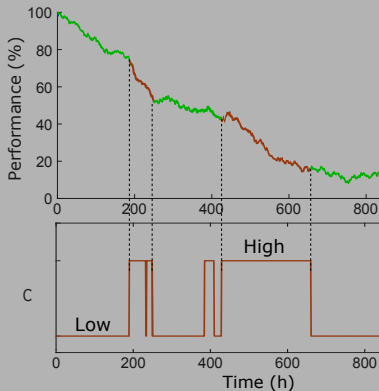
Simulated by a state transition function <sup>2</sup>:

$$x_k = x_{k-1} \cdot \exp(-b_k(c_k) \cdot \Delta t)$$

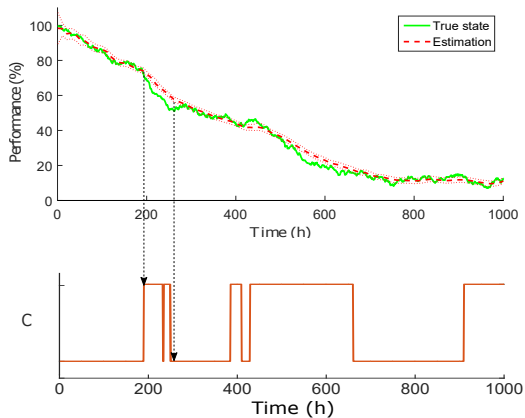
The presence of covariate  $c_k$  impacts the degradation behavior by changing trend parameter  $b_k$ .

<sup>2</sup> An, D., Choi, J.H., and Kim, N.H. (2013). Prognostics 101: A tutorial for particle filter-based prognostics algorithm using Matlab. *Reliab. Eng. Syst. Saf.*, 115, 161-169.

# Degradation example



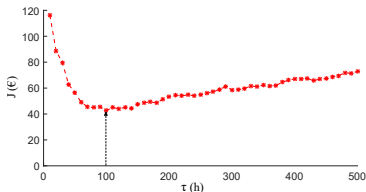
## Degradation estimation examples





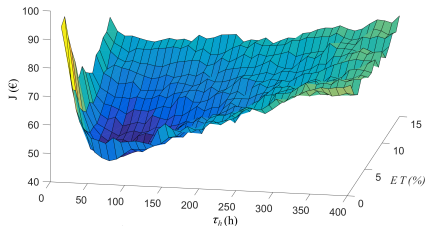
# Decision variables

## Periodic inspection



Inter-inspection period  $\tau^* \simeq 100h$

## Online inspection

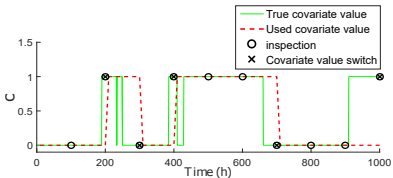


Error threshold  $ET^* = 4\%$

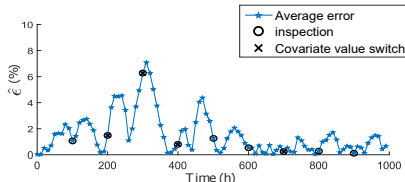
Minimum inter-inspection period  $\tau_h^* = 50h$

# Different inspection schemes

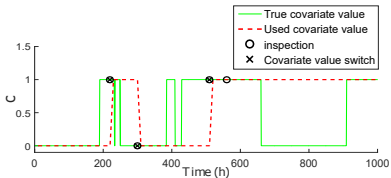
## Periodic covariate inspection



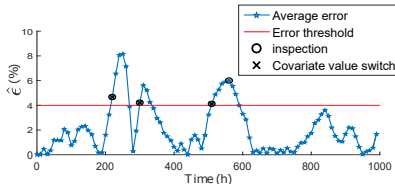
## Error of periodic inspection



## Online covariate inspection

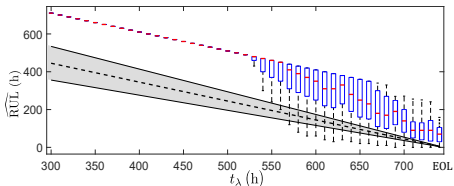


## Error of online inspection

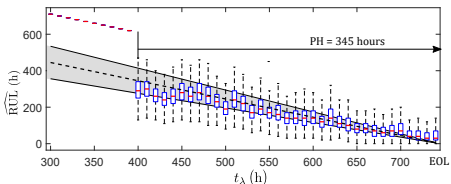


# RUL predictions results

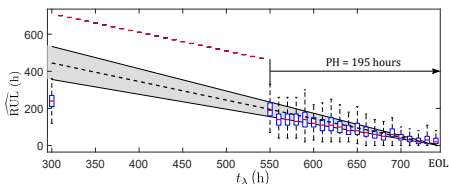
## RUL predictions without inspection



## ~ with periodic inspection



## ~ with online inspection



## Cost and prognostic performance

	Without inspection	Periodic $\sim$	Online $\sim$
$Acc$	0	0.54	0.27
$\alpha Ac$	0	0.53	0.36
$\hat{\epsilon}(\%)$	69.19	20.73	28.91
$N_{ins}$	–	215	110
$J$ (€)	692	422	399

# Summary

Challeng accomplished:

- ▶ RUL prediction using the information from inspections of covariate
- ▶ Two covariate inspection schemes: online and periodic
- ▶ Online inspection scheme helps to minimize the cost by avoiding unnecessary inspection

⇒ A different way of using degradation related information at different levels

## Part IV

# Multi-level Prognostics Using Different Sources of Degradation Information<sup>3</sup>



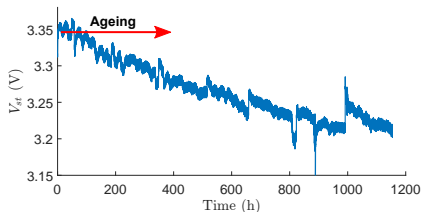
POLITECNICO  
MILANO 1863

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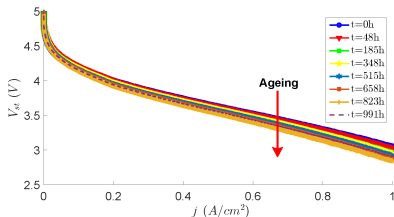
<sup>3</sup>Work in this section has been partly done during an international mobility in the **Laboratory of signal and risk analysis (LASAR)** at *Politecnico di Milano*

# Problem statement

## Stack voltage vs. time



## Polarization measurement



Degradation of a stack observed from different measurements:

- ▶ External measurement: measured frequently, "poor quality" (voltage)
- ▶ Internal characterization: less frequently, "good quality" (polarization)

## Objective

Aggregate RUL predictions from both measurements to improve global RUL quality

# Polarization model

The output voltage of a stack at a given current density  $J$ <sup>4</sup>:

$$V_{st}(J) = n \cdot \left\{ E - r \cdot J - A \cdot \ln\left(\frac{J}{j_0}\right) - m_1 \cdot \exp(m_2 \cdot J) \right\}$$

$V_{st}$ : stack voltage

$n$ : number of cells in the stack

$E$ : open circuit voltage

$r$ : internal resistance

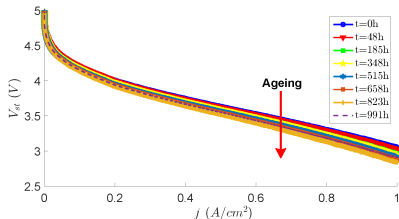
$J$ : operating current density

$A$ : Tafel coefficient

$j_0$ : exchange current density

$m_1$  and  $m_2$ : mass-transfer constants

Time impact on model parameters



<sup>4</sup> J. Larminie and A. Dicks, *Fuel cell systems explained*. Wiley, 2003.

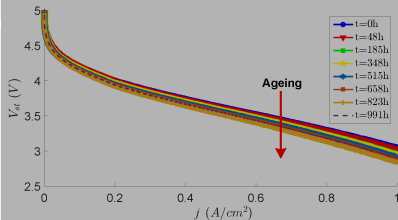
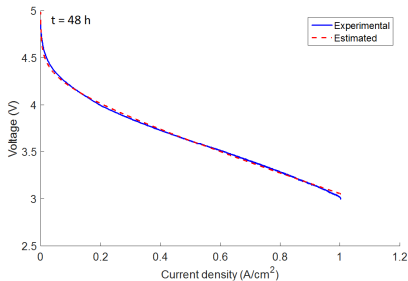


# Polarization model

The output voltage of a stack at a given current density  $J$ <sup>4</sup>:

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## Identify model parameters



<sup>4</sup> J. Larminie and A. Dicks, *Fuel cell systems explained*. Wiley, 2003.

# Polarization model

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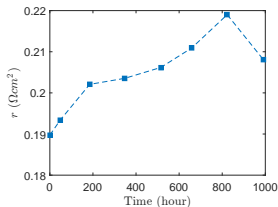
Time impact on model parameters

## Parameters estimation results

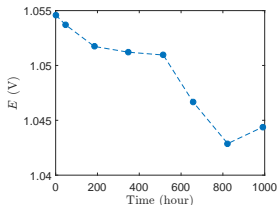
Time (h)	$E$ (V)	$r$ ( $\Omega \text{ cm}^2$ )
0	1,055	0,190
48	1,054	0,193
185	1,052	0,202
348	1,051	0,204
515	1,051	0,206
658	1,047	0,211
823	1,043	0,219
991	1,044	0,208

<sup>4</sup> J. Larminie and A. Dicks, *Fuel cell systems explained*. Wiley, 2003.

# SOH degradation model



$$r(t) = r_0 \cdot (1 + \gamma(t))$$



$$E(t) = E_0 \cdot (1 - \gamma(t))$$

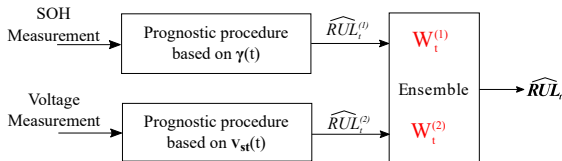
SOH degradation model  $\gamma(t)$  of a PEM fuel cell <sup>5</sup>

- ▶ Definition: degradation rate of  $E(t)$  and  $r(t)$
- ▶ Assumption: availability of a procedure which returns an estimation of  $\gamma(t)$  from polarization measurements

<sup>5</sup> Bressel et al., "Remaining Useful Life Prediction and Uncertainty Quantification of Proton Exchange Membrane Fuel Cell Under Variable Load," *IEEE Trans. Ind. Electron.*, vol.63, no.4, pp.2569-2577, 2016.

# RUL aggregation

- ▶ SOH degradation  $\gamma(t)$
- ▶ Voltage degradation  $V_{st}(t)$  driven by  $\gamma(t)$



$$\widehat{RUL}_t = \sum_{i=1}^M W_t^i \cdot \widehat{RUL}_t^i$$

$$p(\widehat{RUL}_t) = \sum_{i=1}^M W_t^i \cdot p(\widehat{RUL}_t^i)$$

$\widehat{RUL}_t$ : the ensemble outcome for the RUL prediction  
 $\widehat{RUL}_t^i$ : RUL prediction by each  $i^{th}$  individual model  
 $M$ : the number of models

$W_t^i$ : local weights (non-negative and sum to 1).

## Local weight $W_t$ determination

$$\widehat{RUL}_t = W_t^{(1)} \cdot \widehat{RUL}_t^{(1)} + W_t^{(2)} \cdot \widehat{RUL}_t^{(2)}$$

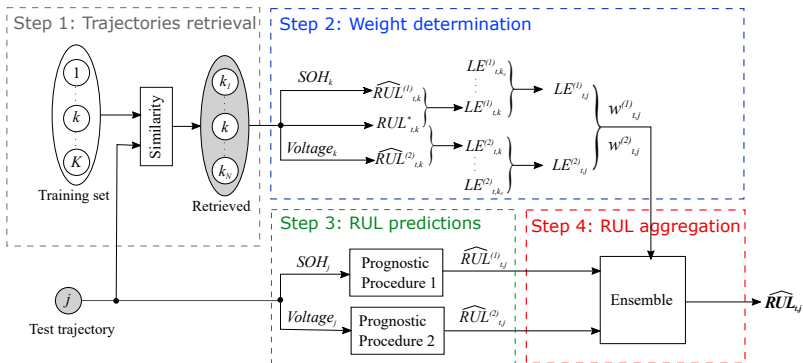
### Why: to benefit from both measurements

- ▶ “good” RUL quality  $\rightarrow$  large weight
- ▶ “poor” RUL quality  $\rightarrow$  small weight

### How

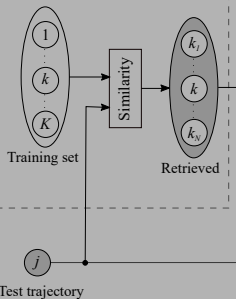
- ▶ Evaluated **locally** on a similar training set (historical data)
- ▶ Weights are recomputed at each time step

# Ensemble-based approach

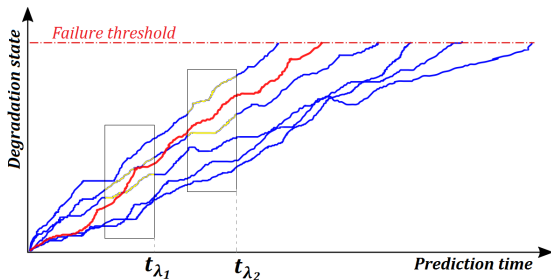


# Ensemble-based approach

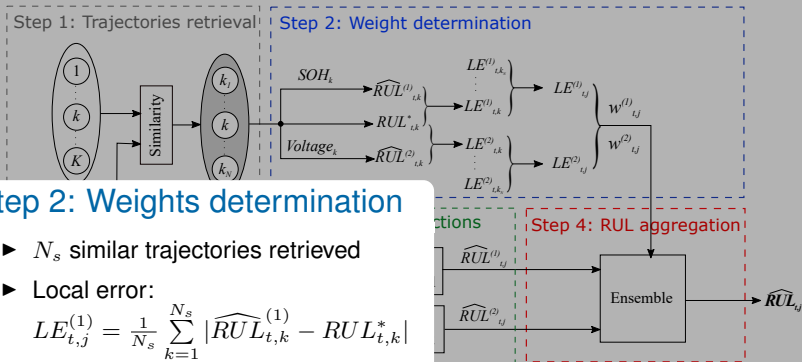
Step 1: Trajectories retrieval



Step 1: Trajectories retrieval



# Ensemble-based approach



## Step 2: Weights determination

- ▶  $N_s$  similar trajectories retrieved

- ▶ Local error:

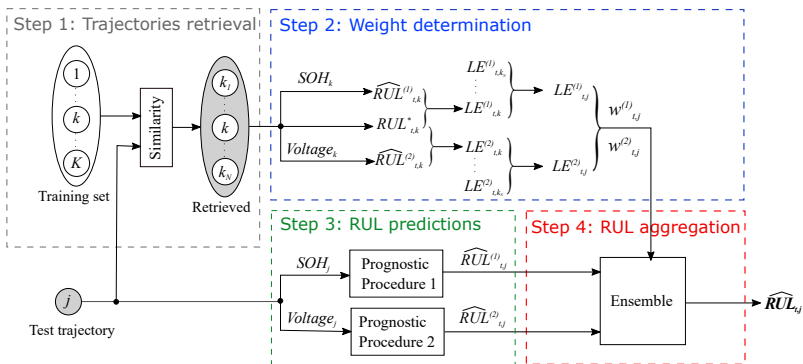
$$LE_{t,j}^{(1)} = \frac{1}{N_s} \sum_{k=1}^{N_s} |\widehat{RUL}_{t,k}^{(1)} - RUL_{t,k}^*|$$

- ▶ Local weight:

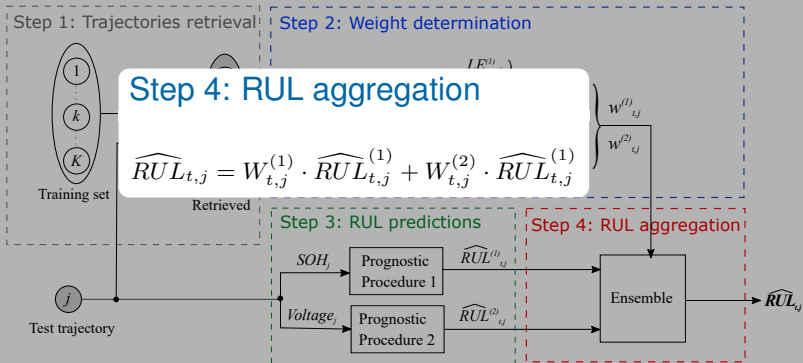
$$W_{t,j}^{(1)} = \frac{1/LE_{t,j}^{(1)}}{1/LE_{t,j}^{(1)} + 1/LE_{t,j}^{(2)}}$$



# Ensemble-based approach



# Ensemble-based approach



# Numerical experiment

## Simulation objective

Produce realistic signals:

- ▶ signal variability and randomness from stack to stack
- ▶ dependency between two types of measurement

## Simulated signals synthesis

- ▶ Two types of measurement:  $\gamma(t)$  and  $V_{st}(t)$
- ▶ Ad hoc simulations based on dependent stochastic processes (Gamma process)

# Simulated signals

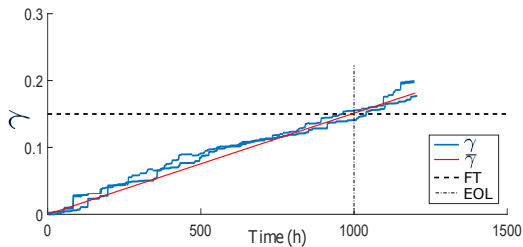
# Simulated signals

- ▶ SOH degradation  $\gamma(t)$

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- ▶ SOH degradation  $\gamma(t)$

## SOH degradation



# Simulated signals

- ▶ SOH degradation  $\gamma(t)$
- ▶ Voltage degradation  $V_{st}(t)$  driven by  $\gamma(t)$

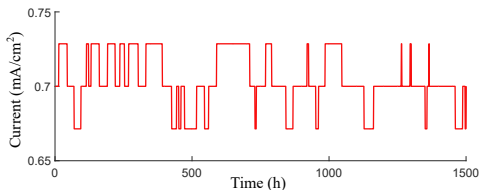
$$V_{st}(t) = f(E(t), r(t), J(t)) \begin{cases} E(t) = E_0 \cdot (1 - \gamma(t)) \\ r(t) = r_0 \cdot (1 + \gamma(t)) \end{cases}$$

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## Loading current





# Simulated signals

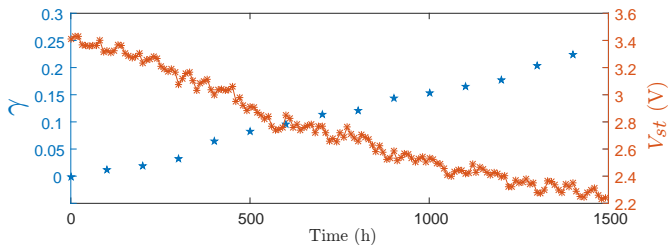
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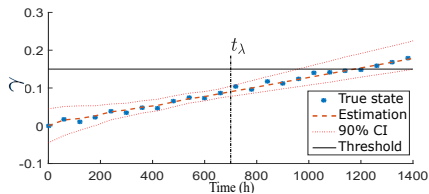
- ▶ SOH degradation  $\gamma(t)$
- ▶ Voltage degradation  $V_{st}(t)$  driven by  $\gamma(t)$

## Measurements $\gamma(t)$ and $V_{st}(t)$

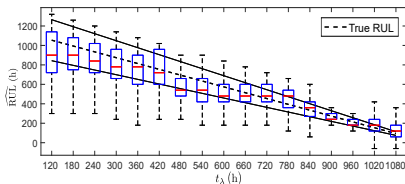


# RUL prediction results

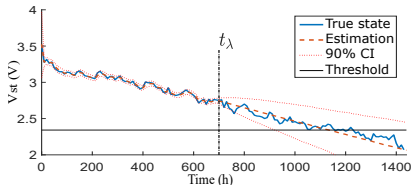
## Estimation of $\gamma(t)$



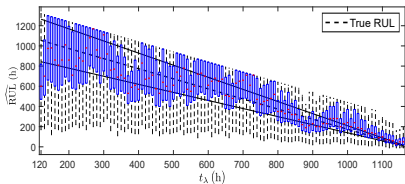
## RUL predictions based on $\gamma(t)$



## Estimation of $V_{st}(t)$

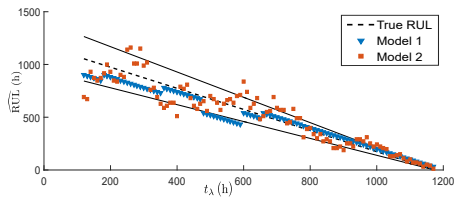


## RUL predictions based on $V_{st}(t)$



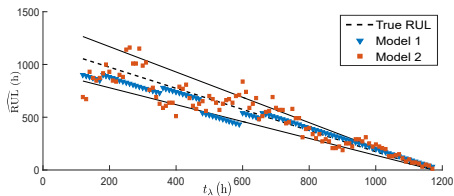
# RUL aggregation

## Individual RUL

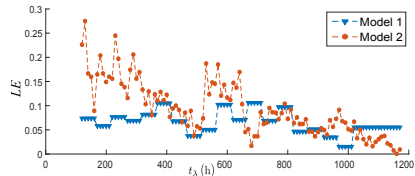


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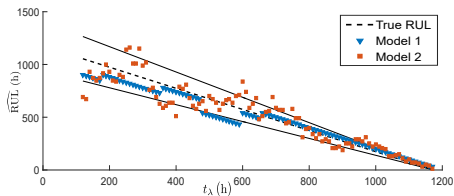


## Local error $LE$

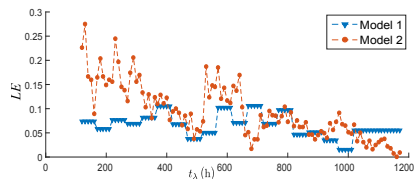


# RUL aggregation

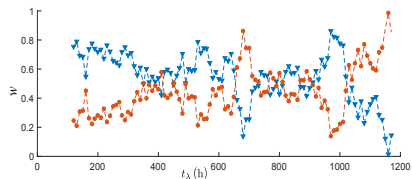
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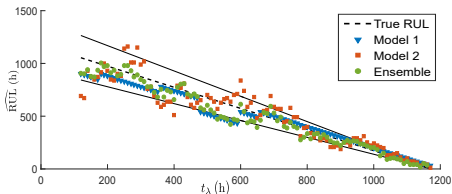


## Local weight $w$

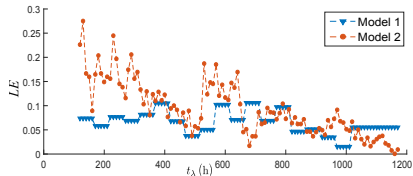


# RUL aggregation

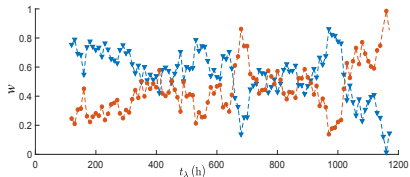
## Aggregated RUL



## Local error $LE$

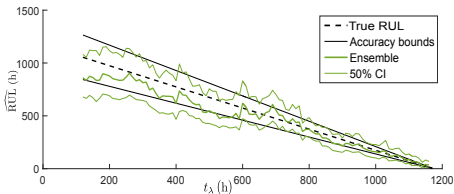


## Local weight $w$

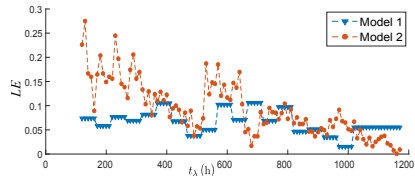


# RUL aggregation

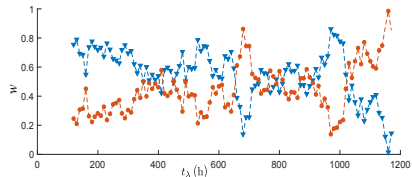
## Aggregated RUL uncertainty



## Local error $LE$



## Local weight $w$





## Performance evaluation

Average performance on 50 test trajectories:

Performance	Model 1	Model 2	Ensemble	
			Point value	PDF
<i>Acc</i>	0.52	0.12	0.55	0.56
$\alpha Ac$	0.31	0.24	0.54	0.49
<i>Std</i>	0.16	0.14	0.07	0.07

\* Prediction quality is improved with different configurations

- ▶ different process variances
- ▶ different signals' dependencies

## Summary

- ▶ RUL prediction quality has been evaluated on historical data
- ▶ Weights have been locally associated to individual predictions from two different measurement signals
- ▶ Aggregated results provided better quality than individual ones
- ▶ Ready for the application in PEM fuel cell when data requirement is met

# Part V

## Conclusion & Perspectives

# General conclusion

## Three main contributions:

- 1 Developed a PF-based approach for RUL prediction of PEM fuel cell using deeper characterization information
- 2 Proposed an online inspection of degradation covariate at different level to adapt RUL prediction
- 3 Proposed an Ensemble-based approach using degradation information at different levels to improve the RUL prediction quality

# General conclusion

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# Perspectives

## Short term

- ▶ Data involves varying usage profile for both development and validation
- ▶ Inspection schemes based on simple cost function  
→ consideration of more impacts, *e.g.* timeliness

## Long term

- ▶ Validation of developed approaches with real-life data should be envisaged to become commercially attractive
- ▶ Not limited to the framework of PEM fuel cell  
→ adapt and extend to other applications



# Thank you !

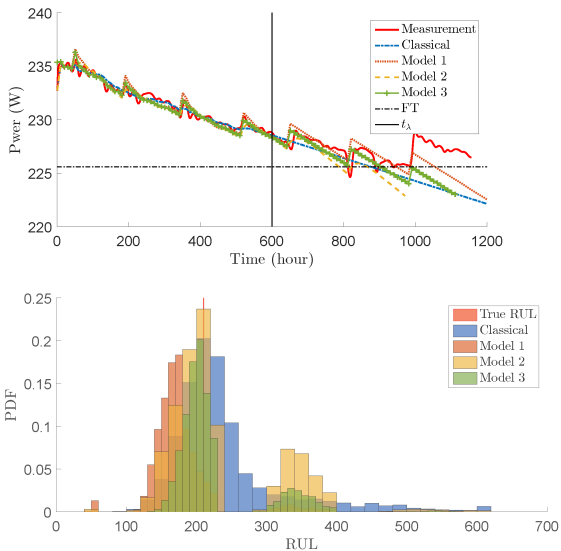
## Publications

- ▶ Zhang D, Cadet C, Yousfi-Steiner N and Bérenguer C (2017) PEMFC RUL Prognostics Considering Degradation Recovery Phenomena. *Journal of Risk and Reliability*, revised.
- ▶ Zhang D, Cadet C, Yousfi-Steiner N and Bérenguer C (2017) A Study of Online Inspection for Multi-level Prognostics. In: *IFAC-PapersOnLine*, 50(1), pp.13716-13721. DOI: 10.1016/j.ifacol.2017.08.2549.
- ▶ Zhang D, Baraldi P, Cadet C, Yousfi-Steiner N, Bérenguer C and Zio E (2017) A Study of Local Aggregation of An Ensemble of Models for RUL Prediction. In: *The 10th International Conference on Mathematical Methods in Reliability (MMR 2017)*, July 3-6, 2017, Grenoble, France.
- ▶ Zhang D, Cadet C, Yousfi-Steiner N, Druart F and Bérenguer C (2017) PHM-oriented Degradation Indicators for Batteries and Fuel Cells. *Fuel Cells*, 17(2), pp.268-276. DOI: 10.1002/fuce.201600075.
- ▶ Zhang D, Cadet C, Yousfi-Steiner N and Bérenguer C (2016) Some Improvements of Particle Filtering Based Prognosis for PEM Fuel Cells. In: *IFAC-PapersOnLine*, volume 49. pp.162-167. DOI: 10.1016/j.ifacol.2016.11.028.
- ▶ Zhang D, Cadet C, Yousfi-Steiner N and Bérenguer C (2015) PHM-oriented degradation indicators for PEM fuel cells: What can be learnt from battery State of Charge estimation . In: *Proc. 6th International Conference on Fundamentals & Development of Fuel Cells*, Paper 190. Feb 2015, Toulouse, France.

# Part VI

## Appendix

# RUL uncertainty



## Proposition 1

Two indicators  $V_{st}(t)$  and  $\gamma(t)$  are generated from the same realization of a Gamma degradation process, with different additive noises.

$$\bar{\gamma}(t) = \bar{\gamma}(t-1) + \Gamma(\bar{\alpha}\Delta t, \bar{\beta})$$

$$\gamma^i(t) = \gamma^i(t-1) + \Gamma(\alpha^i \Delta t, \beta^i)$$

$$\begin{cases} \gamma_1^i(t) = \gamma^i(t) + \mathcal{N}(0, \sigma_1^2(t)) \\ \gamma_2^i(t) = \gamma^i(t) + \mathcal{N}(0, \sigma_2^2(t)) \end{cases} \rightarrow \begin{cases} \gamma_{meas}^i(t) = \gamma^i(t) + \mathcal{N}(0, \sigma_{\omega_1}^2(t)) \\ V_{stmeas}^i(t) = V_{st}^i(t) + \mathcal{N}(0, \sigma_{\omega_2}^2(t)) \end{cases}$$

## Proposition 2

Two indicators  $V_{st}(t)$  and  $\gamma(t)$  are simulated from two different degradation processes, yet the two processes are dependent processes by construction.

$$\begin{array}{l}
 G_1(\alpha_1, \beta) \\
 G_2(\alpha_2, \beta)
 \end{array}
 \rightarrow
 \left\{
 \begin{array}{ll}
 a_1 = \alpha_1 - \rho\sqrt{\alpha_1\alpha_2} & \rightarrow g_1^i(a_1, \beta) \\
 a_2 = \alpha_2 - \rho\sqrt{\alpha_1\alpha_2} & \rightarrow g_2^i(a_2, \beta) \\
 a_3 = \rho\sqrt{\alpha_1\alpha_2} & \rightarrow g_1^i(a_3, \beta)
 \end{array}
 \right\}
 \rightarrow
 \begin{array}{l}
 G_1^i = g_1^i + g_3^i \\
 G_2^i = g_2^i + g_3^i
 \end{array}$$

$$\left\{
 \begin{array}{l}
 \gamma_1^i(t) = \gamma_1^i(t-1) + G_1^i \\
 \gamma_2^i(t) = \gamma_2^i(t-1) + G_2^i
 \end{array}
 \right.
 \rightarrow
 \left\{
 \begin{array}{l}
 \gamma_{meas}^i(t) = \gamma^i(t) + \mathcal{N}(0, \sigma_{\omega_1}^2(t)) \\
 V_{stmeas}^i(t) = V_{st}^i(t) + \mathcal{N}(0, \sigma_{\omega_2}^2(t))
 \end{array}
 \right.$$